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•10	Titles of technical contributions or publications, particularly those in the geophysical sciences, where published.
*11	Brief statement of any special interests or qualifications in the geophysical sciences.
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12. (STUDENT MEMBERS ONLY) The person whose signature appears above is known to me and

☐ He is a full-time student, or ☐ a teaching or research assistant enrolled in more than half of full-time academic program.

(Name of college or university) expected to graduate in\_\_\_\_\_(year) with the degree of\_\_

\_(subject) at-

membership as well.

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\* Applicants for student membership may omit Questions 9, 10, and 11, but must fill in Question Please return form with check or money order payable to American Geophysical Union, 1515 Ma chusetts Ave., N.W., Washington 5, D. C.

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## Detection of Sea-Water Motion by Nuclear Precession

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The long memory of nuclear-spin Larmor precession can be utilized to detect small changes in precession phase angle. The detection of longrange, slow transport of sea water caused by internal waves or other disturbances would seem desirable. Consider how the transport of a volume element of spins in a liquid through a spatial, inhomogeneous, magnetic field affects the phase of Larmor precession. For simplicity, consider a volume element of spins at position  $x_0$  at time t = 0, and assume that this volume element moves with a constant velocity v in an inhomogeneous field H(x). The magnitude and direction of v is to be measured, and it is shown that v as small as 10-1 cm/sec is detectable. The free precession signal [Hahn, 1950] for this element of spins is defined in terms of the vector

$$V(t) = \exp \left[ j\gamma \int_0^t H(x_0 + vt) dt \right]$$

where, at time t,  $vt = x - x_0$ ;  $\gamma$  is the spin gyromagnetic ratio. After writing  $H(x_0 + vt)$ as a Taylor's series and keeping the first two terms for convenience, we obtain

$$V(t) = \exp\left\{j\gamma \int_0^t \left[H(x_0) + \frac{dH}{dx}\Big|_{x_0} vt\right] dt\right\}$$
$$= \exp\left[j\gamma [H(x_0)t + Gvt^2/2]\right]$$

where  $G = (dH/dx)_{z_0}$ .

We see that the presence of a velocity v produces a phase shift in time t given by  $\Delta \varphi =$  $\gamma Gvt^2/2$  (assuming a constant field gradient). In practice, the transport effect can be measured by observing the constructive interference of the various spin volume elements distributed throughout xo. Actually xo should pertain to

a volume, but an analysis in one dimension sufficient to give proper orders of magnitude

Electronic apparatus is necessary here in order to measure spin echoes [Hahn, 1950]. A emi of sufficient volume (a few liters or more, as desired) is immersed and fixed in the sea. A in the Varian magnetometer [Packard and Varian 1954], protons precess in the earth's field attached an initial polarizing field is turned off at t = 1In a time interval from t = 0 to  $t = \tau$ , let the protons precess in a total magnetic field made up of the earth's field H., assumed to be per feetly homogeneous, and the inhomogeneous field H(x), supplied by an appropriate second coil carrying a current I. At time  $t = \tau$ , the current I is reversed to -I, and H(x) change to -H(x). Under these conditions, we solve for the spin echo. It is convenient to assume that the fraction of spins which precess in an inhomogeneous field  $H(x_0)$  at  $x_0$  is given by

$$P(\Delta\omega) = N \exp\left(-\Delta\omega^2/2\Delta\omega_{as}^2\right)$$

where N is a normalizing coefficient,  $\gamma H(x_0)$  =  $\Delta\omega$ ,  $\gamma H_{\bullet} = \omega_{\bullet}$ , and  $\Delta\omega_{\bullet\bullet}^2$  is the mean square deviation in Larmor frequency due to H(x) First we compute the phase behavior of V( in the time intervals 0 to  $\tau$  and from  $\tau$  to twe then average V(t) over  $P(\Delta\omega)$  and look for constructive interference from spin eches at some time  $t_*$  for  $t > \tau$ .

At 
$$t = \tau$$
,

$$V(\tau) = \exp \left[ j(\omega_{\bullet} + \Delta \omega) \tau + j \gamma G v \tau^{2} / 2 \right]$$

For  $t \ge \tau$ , and if we note that  $\Delta \omega$  and  $\theta$ change sign (not the G above) because current I is reversed,

$$\begin{split} \gamma(t) &= \exp\left(+j\omega_{s}t\right) \cdot \exp\left[-j\Delta\omega(t-2\tau)\right. \\ &+ \frac{j\gamma G v \tau^{2}}{2} - j\gamma G v \int_{\tau}^{t} t \ dt \right] \\ &= \exp\left[j\omega_{s}t - j\Delta\omega(t-2\tau)\right. \\ &- j\gamma G v \left(\frac{t^{2}}{2} - \tau^{2}\right)\right] \end{split}$$

The measured or average value of V(t) is

$$\begin{split} \widehat{V(t)} &= \int_{-\infty}^{\infty} P(\Delta \omega) \, V(t, \, \Delta \omega) \, d\Delta \omega \\ &= N(2\pi \overline{\Delta \omega_{o*}}^2)^{1/2} \, \exp \left[ j \omega_{o} t - j \gamma G v \right] \\ &\cdot \left( \frac{t^2}{2} - \tau^2 \right) \right] \exp \left[ -\frac{(t - 2\tau)^2 \Delta \omega_{o*}^2}{2} \right] \end{split}$$

where  $N(2\pi \Delta \omega_{or}^2)^{1/2} = 1$ . A signal maximum occurs essentially at  $t = 2\tau = t_s$ , and the phase shift of this signal, due to the velocity v, is

$$\Delta \varphi = \gamma G v \tau^2$$

The problem now is to measure  $\Delta \varphi$  for a given minimum v to be detected. Assume G = 0.01

 $^{1}$  To some extent a larger G value could be used but V(t) then attenuates because of molecular selfdiffusion [see also Herzog and Hahn, 1956 (appendix). From spin-echo experiments, this produces an attenuation of signal amplitude given by

$$\exp\left[-2/3(\gamma G)^2Dt^2\right]$$

where D is the self-diffusion coefficient. If we let t = 1 sec, and  $D = 2 \times 10^{-5} \text{ cm/sec}^2$  for water, then attenuation, due to self-diffusion, to 1/e of the initial amplitude, is given when  $G \approx 0.01$ gauss/cm. We therefore limit G to this value.

Let  $\tau = 1$  sec, which is approximately the relaxation time for sea water, and let  $\gamma =$  $2.7 \times 10^{\circ}$  for protons. If we wish to detect a velocity  $v = 10^{-1}$  cm/sec, then  $\Delta \varphi \cong 0.3$  radians. This phase shift could be measured simply by beating V(t) against a dummy echo signal from an identical apparatus, where v = 0. In this way it is possible to cancel out fluctuations in H(x) (or I) which would otherwise cause phase shifts exceeding  $\Delta \varphi$ . The echo signal will last for a time

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$$\Delta t = 2\pi/(\Delta \omega_{as}^{2})^{1/2} = 2\pi/\gamma Gl \approx 10^{-3} \text{ sec}$$

where  $l \cong 30$  cm is chosen as the sample breadth. This should be sufficient time for resolution, since it allows an observed free precession at the average frequency  $\omega$ , through at least 10

If two fixed stations are separated over long distances from one another and each station carries out simultaneous measurements, it would be possible to correlate velocities v at the two positions by noting correlations in phase shifts  $\Delta \omega$ . Also the sign of  $\Delta \omega$  would reflect the sign of v. It does not appear feasible to carry out the proposed measurement on a moving platform unless means can be found for correcting or canceling out fluctuations of platform motion to a high degree.

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<sup>1</sup> Instead of reversing I, a radiofrequency put applied for a time to at the average Larmor in quency w. would serve the same purpose. If the field amplitude of the pulse is  $H_1$ , then  $\gamma H_1 t_0 = 1$ is the necessary condition.