

MIDTERM EXAM

Tuesday, October 19, 2004, 3:30 – 4:50pm

please observe the honor code

- This is an **80 minute, open book, open notes** exam. You may use only the Nishimura textbook, class notes, your notes, handouts, and homework. No other written material is allowed. **No calculators.**
- This exam contains **five problems.**
- Unless specified, assume that all RF excitations are applied at the Larmor frequency $\omega = \omega_0$ and that signal demodulation is based on ω_0 , the field strength is 3 Tesla, and we are imaging ^1H (4257 Hz/G).
- **Efficient answers that show insight will be rewarded.**
- **Read each problem carefully.**

3. (10 points) **Sampling Model**

In conventional 2DFT imaging, the acquisitions typically cover a square in k-space with $W = W_{k_x} = W_{k_y}$. Truncation in k_x and k_y produce blurring along x and y . Evaluate the blurring function along the x axis? and along the $x=y$ line (45°)? Is higher resolution achieved along the $x=y$ line? Explain?

4. (30 points) **Off-Resonance in 2D Imaging**

We are imaging a 2D slice. Suppose that the off-resonance within the slice is a linear function of position: $\Delta\omega(x,y) = ax + by$. The acquisition gradients are $G_x(t)$ and $G_y(t)$.

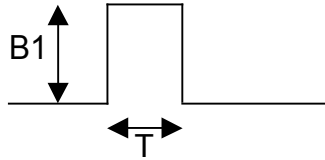
What is the effective k-space trajectory $k_x(t)$, $k_y(t)$?

Hint: Start with the signal equation. The solution should be a function of $G_x(t)$, $G_y(t)$, a , b , and t .

If you know the values of a and b in advance, how would you adjust a 2DFT pulse sequence to make the actual samples fall along a rectangular grid in k-space? Explain in words, or with a sketch.

5. (15 points) **Excitation**

The following RF pulse is called a “hard” pulse:



- Suppose that peak B_1 is limited to 0.16 Gauss. What is the shortest duration, T , which can produce a 90° tip?
- If this pulse were played by itself (no accompanying gradient), and using the small-tip approximation, find an amplitude and duration that produces a 30° tip for water ($\omega=0$) and no tip for lipid ($\omega=-440$ Hz).